

## HOMEWORK VI Solution

1)

One can get the equilibrium fuel cell voltage from the following equation:

$$\varepsilon = \frac{-\Delta G_r(T, P)}{n_e F} \quad \text{Eq.(1)}$$

Note that  $\Delta G_r$  is the function of  $T$  and  $P$ . Using Equil, one can get

$-\Delta G_r(T = 353K, P = 150kPa) = 230kJ / (\text{mole of } H_2)$ . Using Eq.(1), we get

$$\varepsilon = \frac{230kJ / \text{mole}}{2 * 96485C / \text{mole}} = 1.19\text{Volt}$$

2)

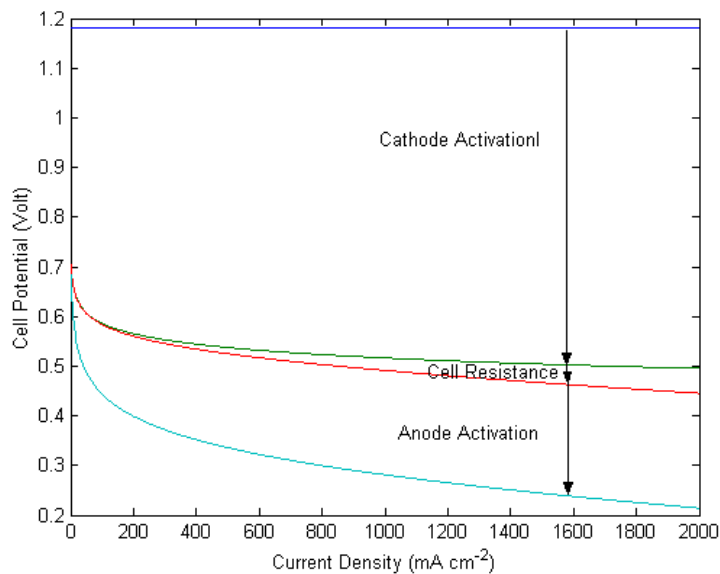
$$\eta_{a, \text{cathode}} = \frac{RT}{\alpha n_e F} \ln\left(\frac{i_{o, \text{cathode}} / A}{i / A}\right)$$

$$\eta_{a, \text{anode}} = -\frac{RT}{(1-\alpha)n_e F} \ln\left(\frac{i_{o, \text{anode}} / A}{i / A}\right)$$

$$\eta_{\Omega} = i \cdot R_{\Omega} = \frac{i}{A} \cdot R_{\Omega} A$$

$$\varepsilon_{\text{cell}} = \varepsilon_r - \eta_{\Omega} - |\eta_{a, \text{cathode}}| - |\eta_{a, \text{anode}}|$$

Assuming  $\alpha = 0.5$ , we get the following plot



3)

$$\eta_{\text{second}} = \frac{W_{\text{out}}}{\Delta H_r} = \frac{\dot{W}_{\text{out}} / A}{\Delta \dot{H}_r / A}$$

$$\Delta \dot{H}_r / A = \Delta \hat{h}_r \cdot \frac{i}{A} \cdot \frac{1}{2F} = 284 \text{kJ/mol} \cdot \frac{1}{2 \cdot 96485 \text{C/mol}} \cdot \frac{i}{A} = 1.47 \cdot 10^{-3} \frac{i}{A} (\text{W/m}^2)$$

$\dot{W}_{\text{out}}$  = current density x cell potential (W/m<sup>2</sup>)

