

# LECTURE 16 — GUIDING/DIRECTING LIGHT <sup>(1)</sup>

OPTOELECTRONICS — electronics + optics

PHOTONICS — optics alone traditionally,  
now — optoelectronics, too.

ELECTRO-OPTIC —  $n(\vec{E})$

NEW COMPONENTS — laser transistors, now

✓ WIRES for light

✓ SOURCES — LEDs, LDs

✓ DETECTORS —

✓ MODULATORS

✓ INTEGRATION

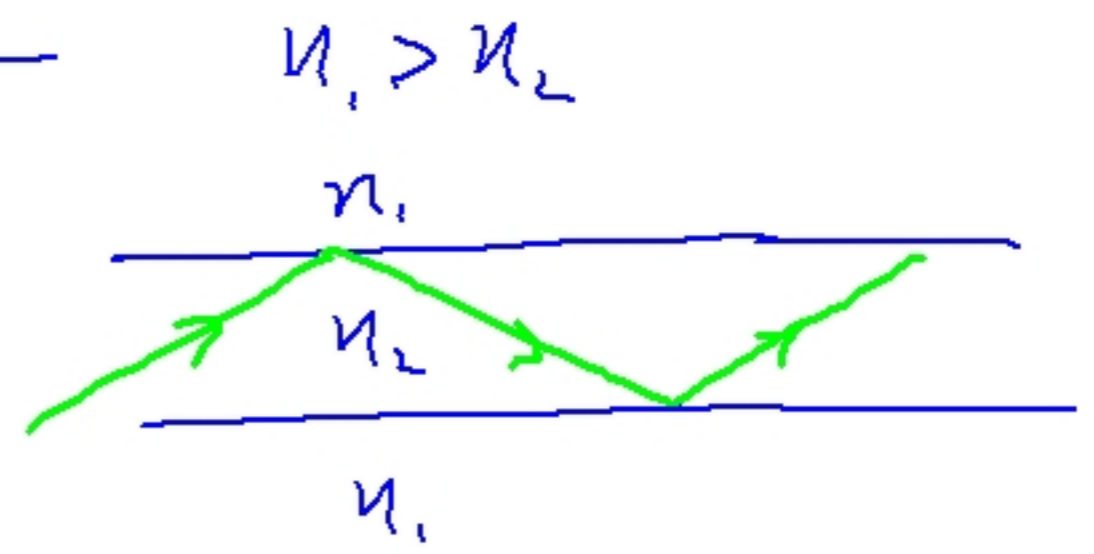
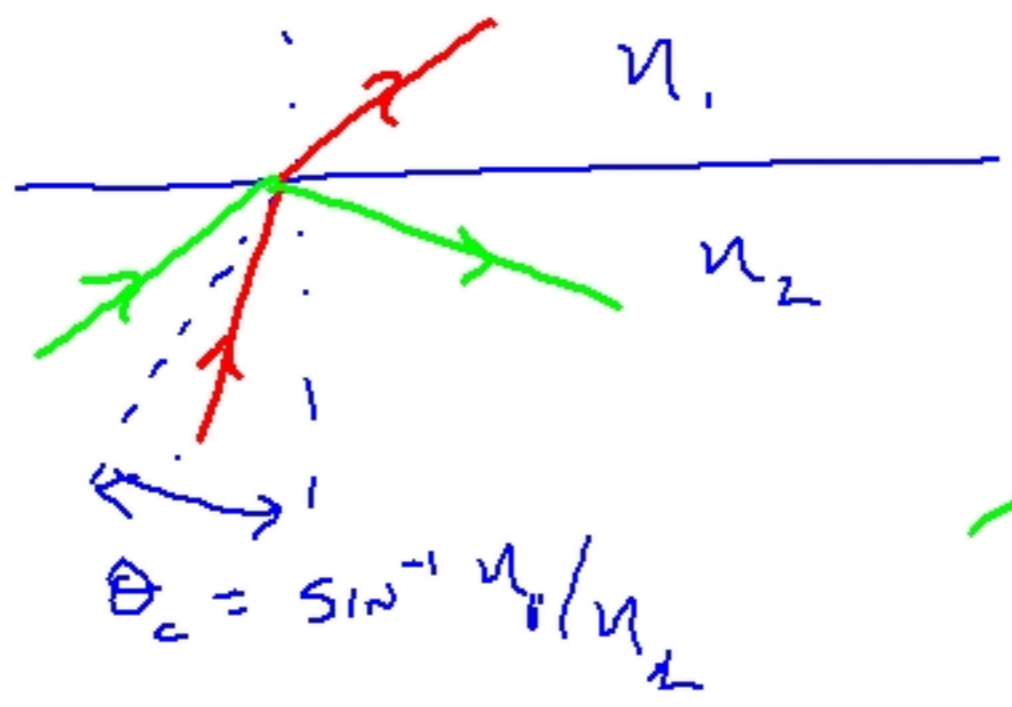
electric in  $\rightarrow$  optical out  
optical in  $\rightarrow$  electrical out

# DIRECTING / GUIDING LIGHT

✓ Free space optics  
lenses, mirrors, holographic elements

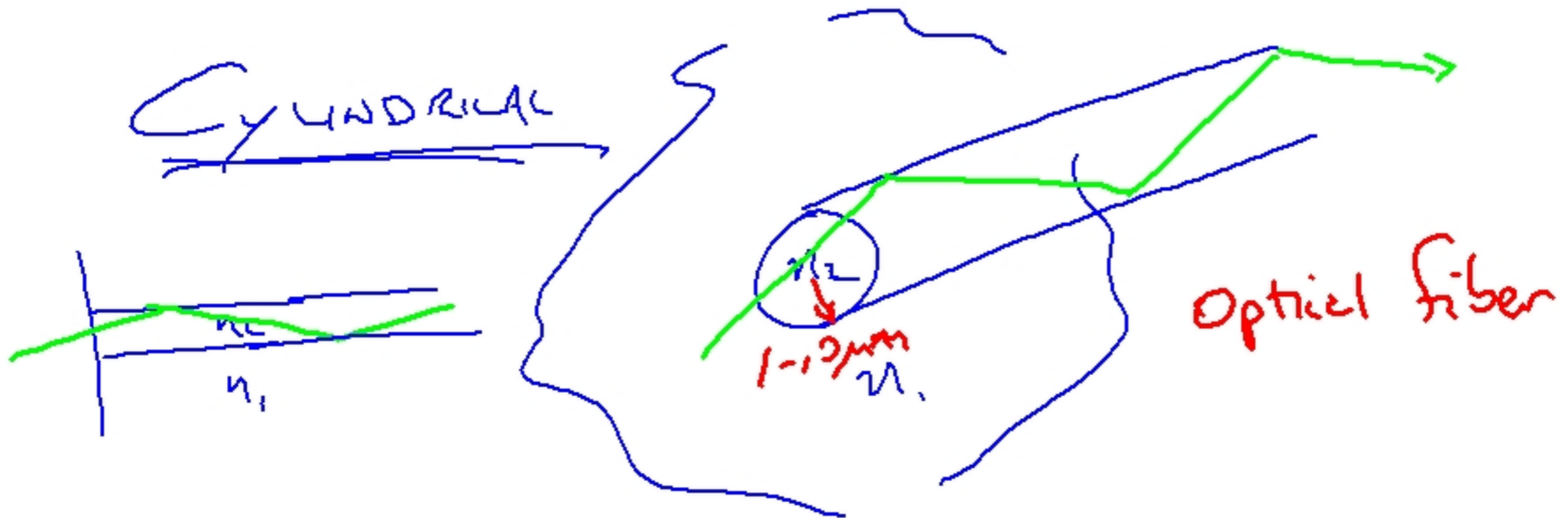
✓ Dielectric waveguides

⇒ based on total internal reflection

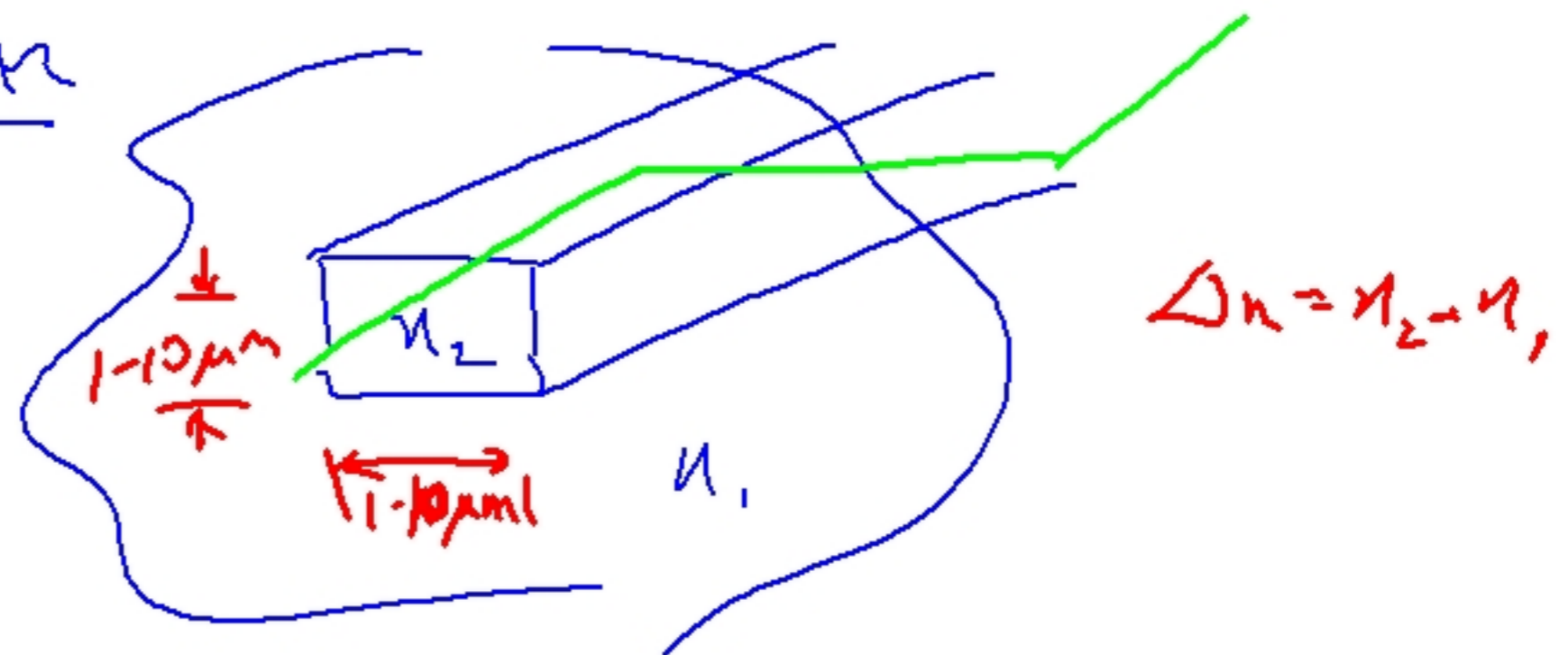


# TWO GEOMETRIES

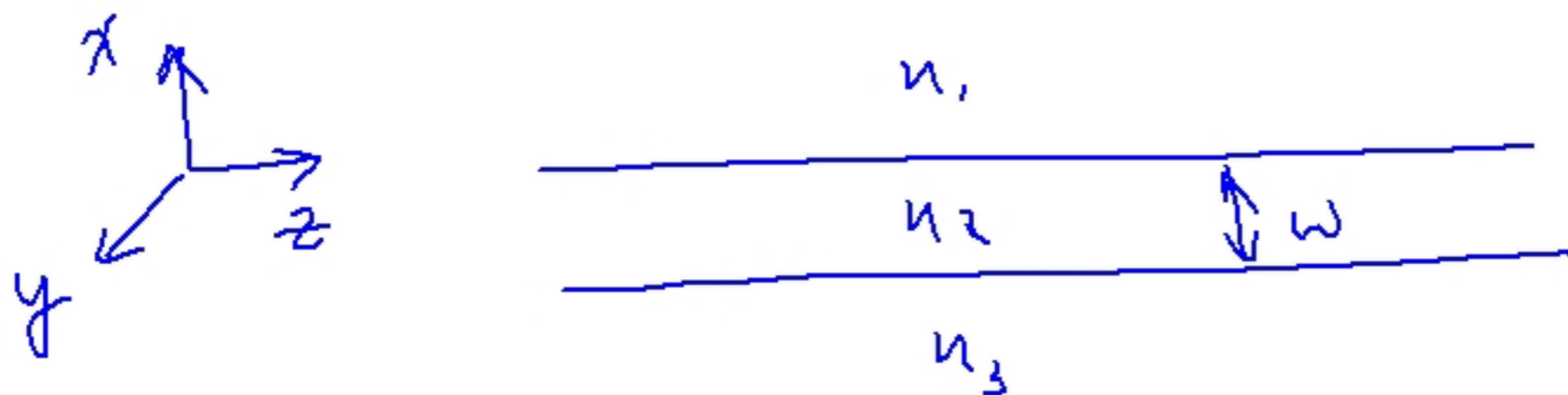
## CYLINDRICAL



## RECTANGULAR



# SLAB WAVEGUIDE



only  $n(x)$

TE wave traveling in  $z$ -direction

$$E_y(x, z, t)$$

$$H_z = H_x$$

SATISFIES

$$\frac{d^2 E_z}{dx^2} + \frac{d^2 E_y}{dz^2} = \mu_0 \epsilon_0 \frac{d^2 E_y}{dt^2}$$

We can write

$$E_y = X(x) Z(z) T(t)$$

$$T(t) = \operatorname{Re} [A e^{-j\omega t}] \quad \omega \text{ is "known"}$$

$$Z(z) = \operatorname{Re} [e^{j\beta_n z}]$$

Leaving

$$\frac{d^2 X_n(x)}{dx^2} - (\beta_n^2 - \mu_0 \epsilon_i \omega^2) X_n(x) = 0$$

↑  
region index (1, 2, 3)

$n = \text{mode index}$

$$\mu_0 \epsilon_i = \mu_0 \epsilon_0 \epsilon_{r_i} \quad \text{where} \quad \epsilon_{r_i} = n_i^2$$

$$\mu_0 \epsilon_i \omega^2 = \mu_0 \epsilon_0 n_i^2 \omega^2 \quad k_0^2 = \left( \frac{2\pi}{\lambda_0} \right)^2 = \frac{\omega_0^2}{c^2}$$

(6)

$$\frac{d^2 X_m(x)}{dx^2} = (\beta_m - \underline{n_i^2 k_0^2}) X_m(x) = 0$$

$$\hookrightarrow k_0 = \underline{2\pi/\lambda_0}$$

$X_m(x)$ : Decaying exponentials if  
 $\beta_m > n_i^2 k_0^2$

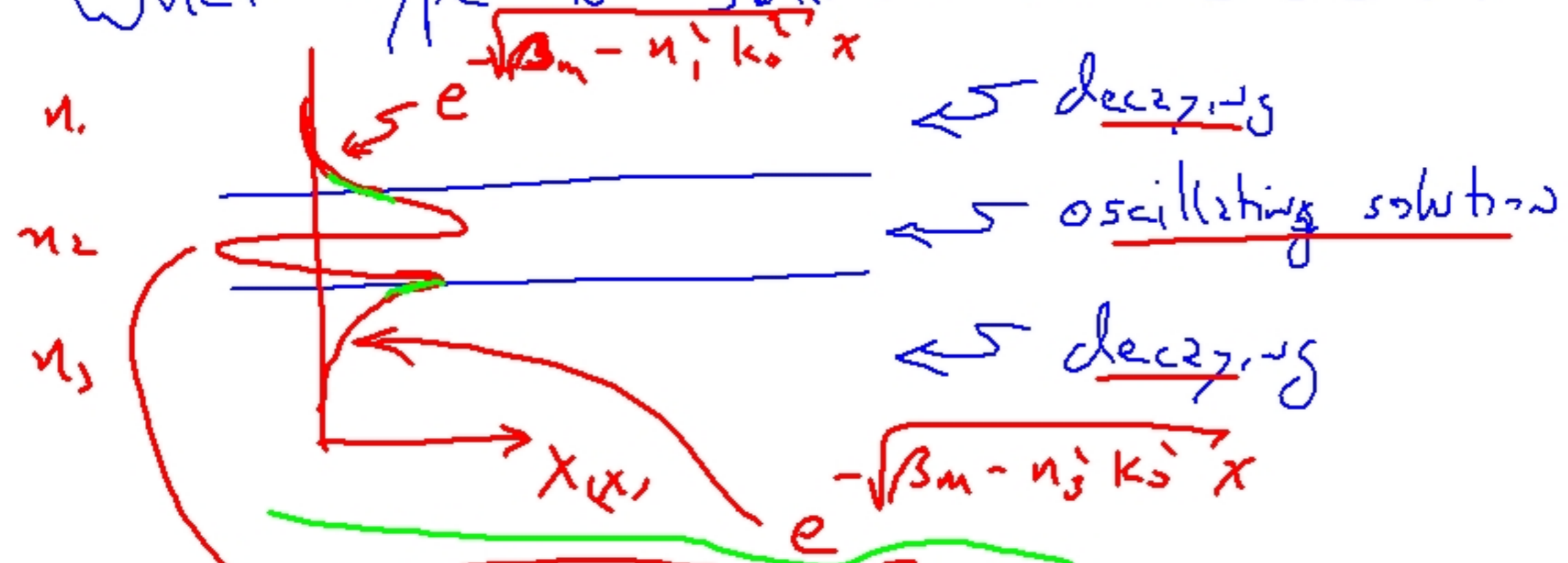
: Oscillating function if  
 $\beta_m < n_i^2 k_0^2$

Recall:

$$Z(z) = \text{Re} [e^{+j\beta_m z}]$$

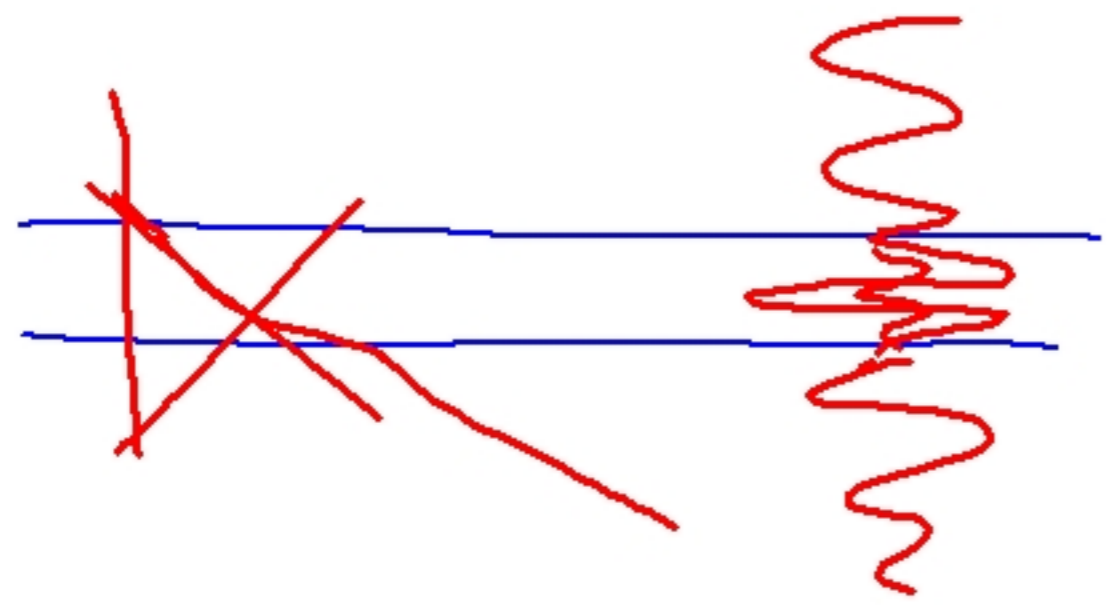
$$T(t) = \text{Re} [A e^{-j\omega t}]$$

What type of solution do we want?



$Re \left[ e^{i \left[ n_2^2 k_0^2 - \beta_m \right] x} \right]$

⇒ Looking for the  $\beta_m$ 's that make the work.



③

$\beta_m$

$$Z(z) T(t) = \text{Re} \left[ A e^{i[\beta_m z - \omega t]} \right]$$

$$v_g = \frac{c}{n_i}$$

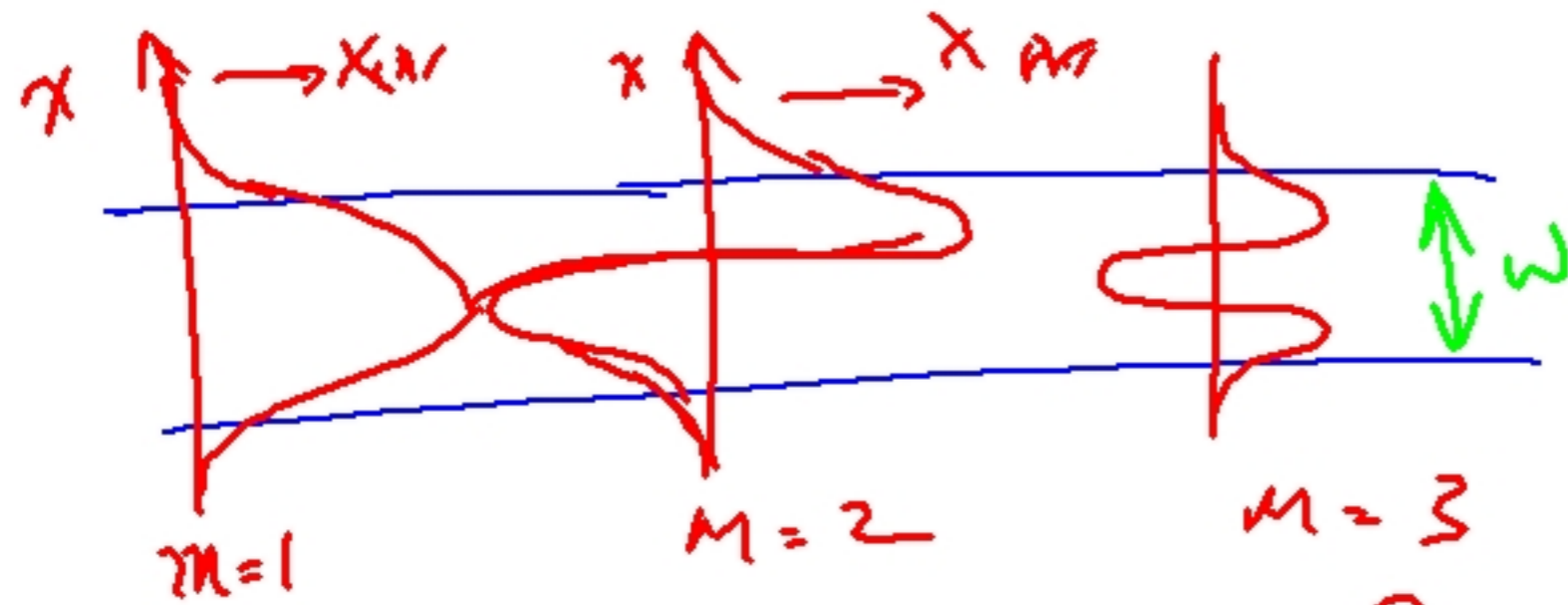
$$v_{\text{eff},m} = \frac{\beta_m}{k_0^2}$$

$v_{\text{eff},m}$

Single mode guide  $\Rightarrow$  only one  $\beta_1$

$\Rightarrow$  only one  $v_{\text{eff}} \Rightarrow$  all light travels at same velocity down guide





mode # = # of oscillations in guide

### General observations

As  $w \uparrow$ , # of modes  $\uparrow$   
 As  $w \downarrow$ , # of modes  $\downarrow$   
 As  $\Delta n \uparrow$ , # of modes  $\uparrow$   
 As  $\Delta n \downarrow$ , # of modes  $\downarrow$

(1)

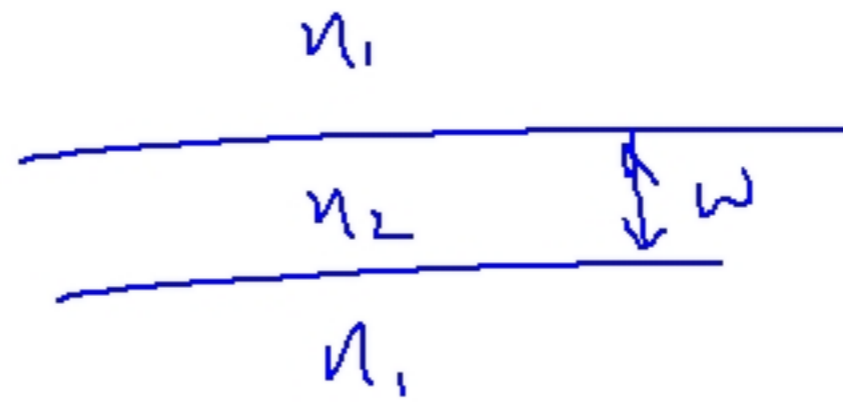
$\therefore$  to get single mode

$\Rightarrow$  narrow guide and/or  
small  $\Delta n$

but narrow guides are harder to  
make & harder to get light into,

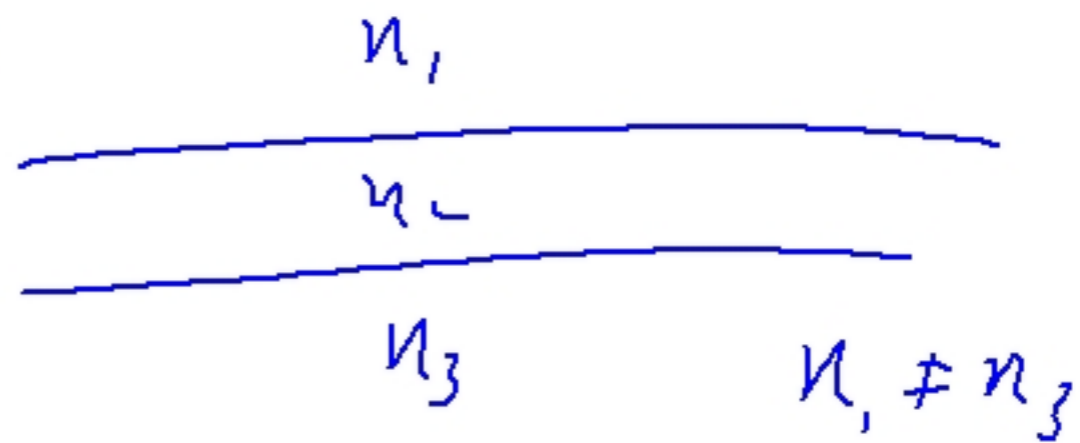
and guides with small  $\Delta n$  are  
not guiding the light strongly  
[ie. are "weakly" guiding]

# Symmetrical guide



find min  $w$  for guiding

# Asymmetrical guide



Air  $n=1$

Input



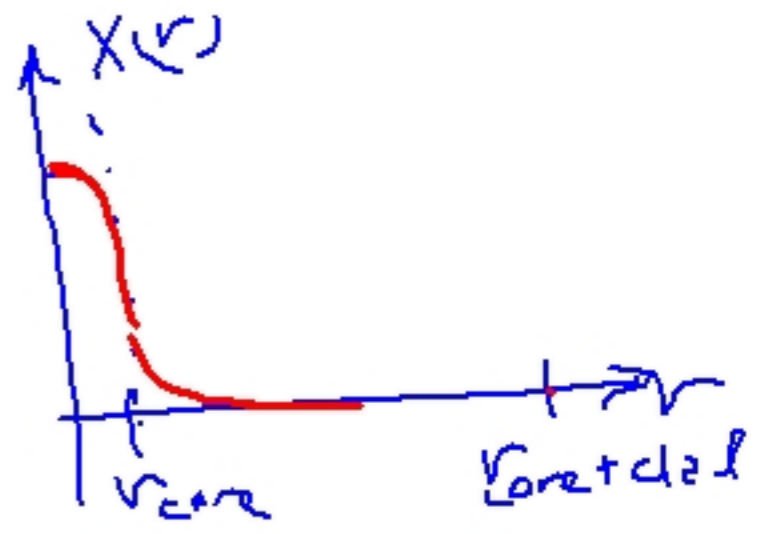
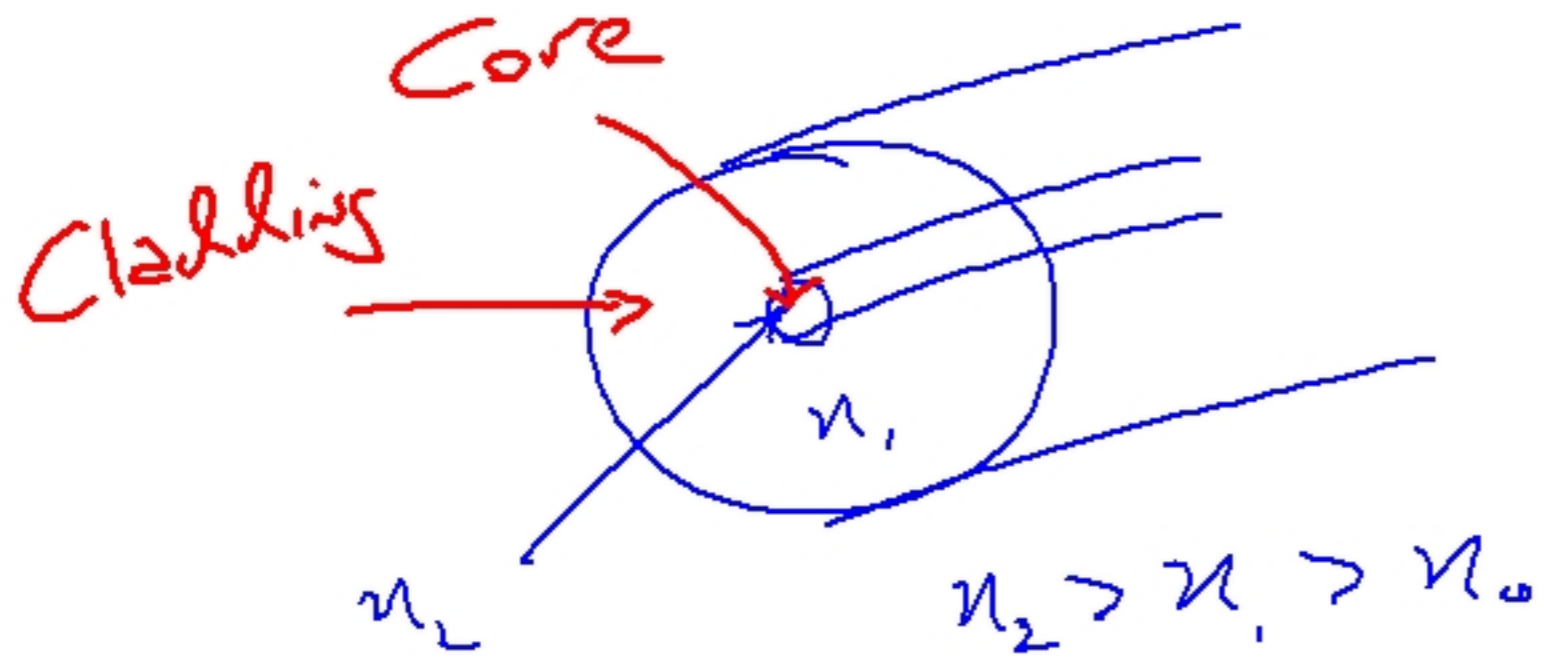
Input



→ here there is a minimum  $w$

# TWO-DIMENSIONAL CONFINEMENT

## 1. CYLINDER [Fiber]



### Bare core



no good  
unprotected  
( $\Delta n$  very large too)

# Rectangular guides

$n_1$	$n_2$	$n_3$
$n_4$	$n_5$	$n_6$
$n_7$	$n_8$	$n_9$

$$n_5 > n_{1,2,3,4,6,7,8,9}$$

often

$$\begin{aligned} n_1 &= n_3 \\ n_7 &= n_9 \\ n_4 &= n_6 \end{aligned}$$

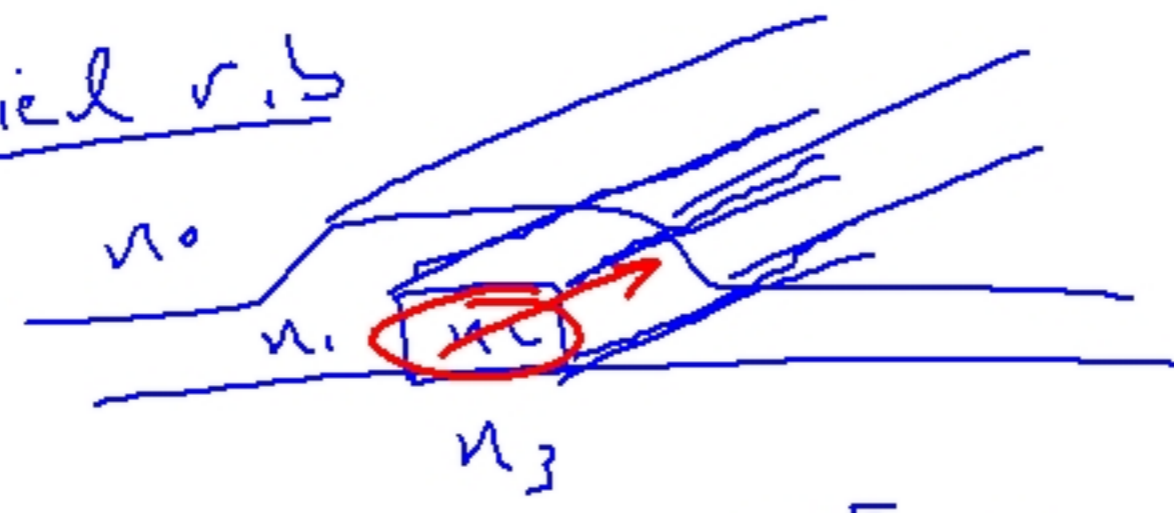
$n_1$	$n_2$	$n_3$
$n_4$	$n_5$	$n_6$
$n_7$	$n_8$	$n_9$

## Examples

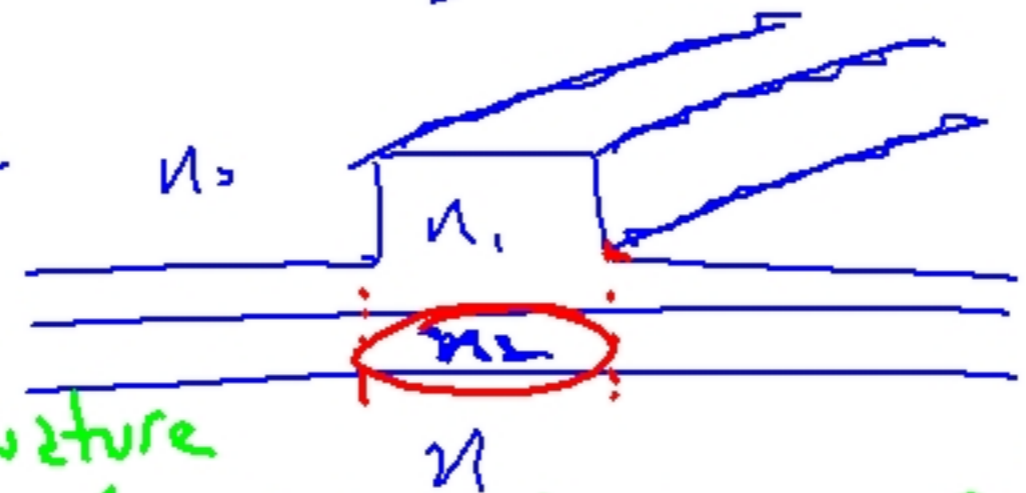


Rib guide

② Buried r.i.b



③ Ridge



GrAA	INP
GrA	INrAP
GrAA	INP

⇒ induced nature  
 of guiding reduces sensitivity to edge roughness

④ Ion Implanted / Diffused

