**R13** 

## Code No: 113BT

# JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD B.Tech II Year I Semester Examinations, December-2014 PROBABILITY THEORY AND STOCHASTIC PROCESSES

(Electronics and Communication Engineering)

Time: 3 Hours Max. Marks: 75

Note: This question paper contains two parts A and B.

Part A is compulsory which carries 25 marks. Answer all questions in Part A. Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b, c as sub questions.

10 to		Part- A		(25 Marks)
1.a)	What are the axioms of	of probability?		[2M]
b)	Explain the types of R	andom variables.	*	[3M]
c)	Write the properties of	f probability distribution f	unction?	[2M]
d) ·	A Continuous random	given		
		$0 \le x \le 1$ . Find a such that P		[3M]
e)	Define Marginal distri	bution & Marginal density	Functions.	[2M]
f)	Statistically independe	ent Random Variables X a	nd Y have moments	
	$m_{20}=14$ , $m_{02}=12$ , $m_{11}$			[3M]
g)	State any 2 properties	of Cross Correlation Func	tion.	[2M]
h)	For the given aut	o correlation function	for a stationary	process is
	$Rxx(\tau) = 25 + \frac{4}{1 + 6\tau^2}$	Find the mean and varian	ce.	[3M]
i)	State any 2 properties	of the power density spect	rum?	[2M]
j)	Write Wiener-Khinchi	ne relations?		[3M]
		Part-B		(50 Marks)

- 2.a) A binary communication channel carries data as one of the two types of signals denoted by 0 and 1. Owing to noise a transmitted 0 is sometimes received as 1 and a transmitted 1 is sometimes received as a 0. For a given channel, assume a probability of 0.94 that a transmitted 0 is correctly received as a 0 and a probability of 0.91 that a transmitted 1 is received as a 1. Further assume a probability of 0.45 of transmitting a 0. If a signal is sent, Determine
  - (i) Probability that a 1 is received.
  - (ii) Probability that a 0 was received
  - (iii) Probability that a 1 was transmitted, given that a 1 was received
  - (iv) Probability that a 0 was transmitted, given that a 0 was received
  - b) State Random Variable with suitable example.

## OR

- 3.a) State and Prove the Bayes theorem of probability.
  - b) Let  $A_1$ ,  $A_2$ ,  $A_3$  are 3 mutually exclusive and exhaustive events associated with experiment  $E_1.B_1$ ,  $B_2$ ,  $B_3$  are 3 mutually exclusive and exhaustive events associated with experiment  $E_2$ .

1	B <sub>1.0</sub>	B <sub>2</sub>	B <sub>3</sub>	p(Aj)
$A_1$	3/36	*	5/36	*
$A_2$	5/36	4/36	5/36	14/36
A <sub>3</sub>	*	6/36	*	*
P(Bj)	12/36	14/36	*	*

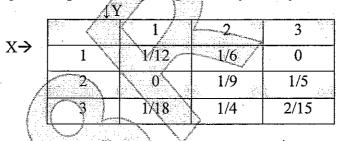
- i. Find missing Probabilities
- ii.  $P(B_3/A_1)$  and  $P(A_1/B_3)$
- iii.  $A_1,B_1$  are independent or not
- 4.a) Explain any 4 Properties of Probability Distribution Function.
  - b) A Continuous random variable X defined by a probability density function given by  $f(x) = 5(1-x^4)/4$   $0 \le x \le 1$ . Find E[X], E[X<sup>2</sup>] and Variance.

## OR

- 5.a) Find mean and variance of Uniform Random Variable.
  - b) Find the characteristic function and first moment for

$$f_X(x) = (1/b)\exp(-(x-a)/b)$$
  $x \ge a$   
= 0 else

6.a) Following table represent the joint probability density function



- (i). Evaluate the marginal distribution of X and Y.
- (ii). Conditional distribution of X given Y=2.
- (iii). Conditional distribution of Y given X=3.
- (iv).  $P(X \le 2, Y = 3), P(Y \le 2), P(X+Y < 4)$
- b) Two random variables X and Y have joint characteristic function  $\Phi_{X,Y}(\omega_1,\omega_2) = \exp(-2\omega_1^2 8\omega_2^2)$

Show that X and Y are zero mean random variables and uncorrelated

### OR

- 7.a) Two random variables  $Y_1$  and  $Y_2$  related to arbitrary random variables X and Y by co-ordinate rotation  $Y_1 = X\cos\theta + Y\sin\theta$ ,  $Y_2 = -X\sin\theta + Y\cos\theta$ .
  - i) Find the covariance function of  $Y_1$  and  $Y_2$ .
  - ii) For what value of  $\theta$ , the random variables  $Y_1$  and  $Y_2$  are uncorrelated
  - b) The joint probability density function of f(x,y) is given by  $f(x,y)=Ae^{-(x+y)}$   $0 \le x \le y$ ,  $0 \le y \le \infty$ 
    - (i). Find the value of A
    - (ii). Find the marginal density of X and Y.
    - (iii). Verify that whether X and Y are independent.

8.a) Statistically independent zero mean Random process X(t) and Y(t) having auto correlation function  $R_{XX}(\tau) = \exp(-|\tau|)$  and  $R_{YY}(\tau) = \cos(2\pi\tau)$  respectively. Find Cross correlation function (CCF) of  $W_1(t)$  and  $W_2(t)$  if

 $W_1(t) = X(t) + Y(t)$  and  $W_2(t) = X(t) - Y(t)$ 

b) State any 4 Properties of Auto Correlation Function

### OR

- 9.a) Prove that random process  $X(t)=A \cos(\omega_c t + e)$  is a wide sense stationary process if it is assumed that A,  $\omega_c$  are constants and e is uniformly distributed over interval  $0 \le e \le 2\pi$ 
  - b) Derive the Mean & Mean -Squared value of output response of a linear system.
- 10.a) Explain any 4 Properties of Power Density Spectrum.
  - b) Derive the power density spectrum of output of a system, in terms of its input PSD.

### OR

- 11.a) Derive the relationship between Cross PSD & Cross Correlation Function.
  - b) The PSD of random process is given

\$16.

13.3

