

**JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD**  
**M.TECH I SEMESTER EXAMINATIONS, APRIL/MAY-2012**  
**STATE AND PARAMETER ESTIMATION THEORY**  
**(CONTROL SYSTEMS)**

Time: 3hours

Max. Marks: 60

**Answer any five questions**  
**All questions carry equal marks**

- - -

- 1.(a) Explain the Maximum-Likelihood method for parameter estimation.  
 (b) Consider the following observations of a scalar parameter  $\theta$ :  

$$z_i = \theta + n_i; \quad i=1,2, \dots, L$$
 where the  $n_i$ 's are independent and identically distributed Gaussian random variables with zero mean and variance  $\sigma^2$ . Estimate the parameter  $\theta$  through Maximum – Likelihood method.
- 2.(a) Explain the Bays estimation criterion for parameter estimation.  
 (b) Find the minimum mean square estimator for the scalar parameter  $\theta$  based on the scalar observation:  $z = \ln \theta + n$   
 where 
$$p(\theta) = \begin{cases} 1 & 0 \leq \theta \leq 1 \\ 0 & \text{otherwise} \end{cases} \quad \text{and} \quad p(n) = \begin{cases} e^{-n} & n \geq 0 \\ 0 & \text{otherwise} \end{cases}$$
3. Derive the necessary relations for parameter estimation using (i) conditional mode estimator and (ii) Maximum a posteriori estimator.
- 4.(a) Explain the relationship of estimators.  
 (b) Explain the procedure for parameter estimation using absolute value cost function.
- 5.(a) Explain the procedure of nonlinear estimation of parameters.  
 (b) Suppose that a message has probability density  

$$p(\theta) = \begin{cases} 1 & 0 \leq \theta \leq 1 \\ 0 & \text{otherwise} \end{cases} \quad \text{and}$$
 That it is observed by the observation  $z = \ln \frac{1}{\theta} + n$   
 where the noise has probability density 
$$p(n) = \begin{cases} e^{-n} & n \geq 0 \\ 0 & n < 0 \end{cases}$$
  
 Find the conditional mean estimate.
- 6.(a) Explain an efficient estimators and derive their relations.  
 (b) Explain asymptotic properties of estimators.
- 7.(a) With suitable diagram explain the Kalman filter and explain how it can be used for state estimation.  
 (b) Explain that identification as Kalman filtering problem.
- 8.(a) Explain what are modifications are to be done in Kalman filter to use it for nonlinear systems.  
 (b) Explain fixed point and fixed log smoothing.