

## JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B.Tech II Year I Semester Examinations, February/March - 2016

## MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE

(Common to CSE, IT)

Time: 3 Hours

Max. Marks: 75

Note: This question paper contains two parts A and B.

Part A is compulsory which carries 25 marks. Answer all questions in Part A.

Part B consists of 5 Units. Answer any one full question from each unit.

Each question carries 10 marks and may have a, b, c as sub questions.

## PART- A

(25 Marks)

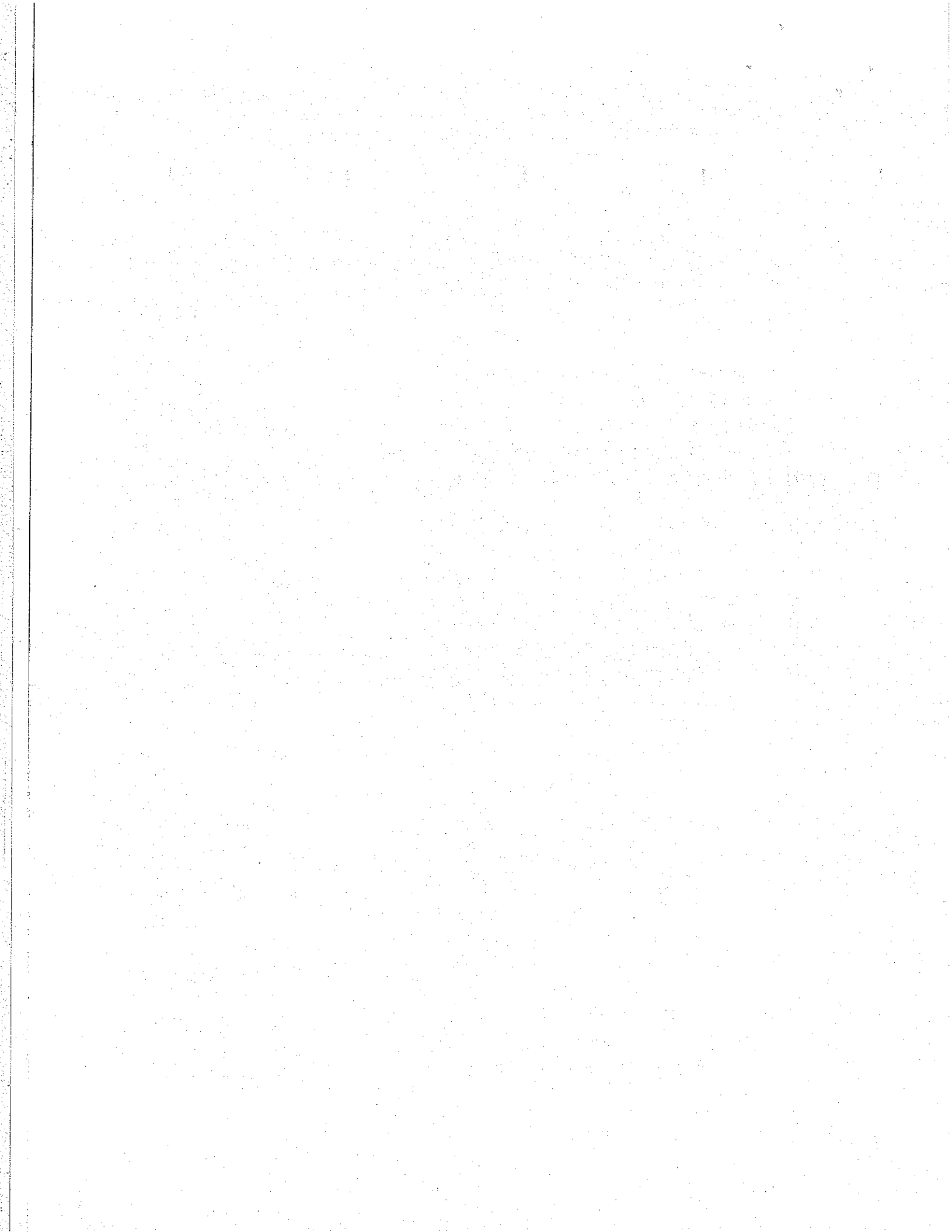
- 1.a) Construct the truth tables of the following formulas.  
 $(P \leftrightarrow Q) \leftrightarrow ((P \wedge Q) \vee (\sim P \wedge \sim Q))$  [2]
- b) Write Converse, Opposite, Contrapositive of the statement "If lines AB and CD are parallel, then the alternative interior angles are equal". [3]
- c) Let  $f: R \rightarrow R$  and  $g: R \rightarrow R$ , where  $R$  is the set of real numbers. Find  $f \circ g$  and  $g \circ f$ , where  $f(x) = x^2 - 2$  and  $g(x) = x + 4$ . [2]
- d) What equivalence relation corresponds to the partitions  $\{ \{1,3\}, \{2\} \}$  [3]
- e) Determine the coefficient of  $x^5 y^{10} z^{10}$  in  $(x - 7y + 3z)^{25}$  [2]
- f) A group of 8 scientists is composed of 5-psychologists and 3-sociologists, In how many ways can a committee of 5 be formed that has 3-psychologists and 2-sociologists. [3]
- g) Use substitution method to solve  $T(n) = T(n-2) + 1$ , where  $T(1) = 1$ . [2]
- h) Solve the following recurrence relations using generating functions.  
 $a_n - 6a_{n-1} = 0$  for  $n \geq 1$  and  $a_0 = 1$ . [3]
- i) Define Euler's Path and Euler Circuit. [2]
- j) What is circuit rank?  $G$  is a connected graph with  $n$  vertices and  $m$  edges, then find circuit rank of  $G$ . [3]

## PART- B

(50 Marks)

2. Obtain the PDNF and PCNF of the following formulas.  
 $P \vee (\sim P \rightarrow (Q \vee (\sim Q \rightarrow R)))$  [10]
- OR**
- 3.a) Show that  $G \vee H$  can be derived from the premises  $B \wedge C, (B \leftrightarrow C) \rightarrow (H \vee G)$ .  
 b) Derive  $P \rightarrow (Q \rightarrow R), Q \rightarrow (R \rightarrow S) \Rightarrow P \rightarrow (Q \rightarrow S)$  (Use CP rule if necessary). [5+5]
- 4.a) Let  $G$  be the set of real numbers not equal to -1 and  $*$  be defined by  $a * b = a + b + ab$ .  
 Prove that  $\langle G, * \rangle$  is an abelian group.  
 b) Define equivalence relation. Show that  $R = \{(x, y) / x \equiv y \pmod{m}\}$  is equivalence relation. [5+5]

OR



5.a) Let  $f : R \rightarrow R$  be defined by

$$f(x) = \begin{cases} x+7 & \text{for } x \leq 0 \\ -2x+5 & \text{for } 0 < x < 3 \\ x-1 & \text{for } x \geq 3 \end{cases}$$

Find (i)  $f^{-1}(-10)$  (ii)  $f^{-1}(8)$  (iii)  $f^{-1}(4)$  (iv)  $f^{-1}(6)$ .

b) Draw the Hasse diagram for the divisibility on the set  $\{1, 2, 3, 4, 8, 16, 28, 32, 64\}$ . [5+5]

6.a) 3 Americans, 3 Mexicans, 3 Canadians are to be seated in a row. How many ways can they be seated so that, no 3 countrymen sit together?

b) How many ways can we distribute 14 indistinguishable balls in 4 numbered boxes so that each box is non empty. [5+5]

OR

7.a) In how many ways can the letters  $\{4.a, 3.b, 2.c\}$  be arranged so that all the letters of the same kind are not in a single block?

b) Expand the multinomial  $(x+y+z)^6$  [5+5]

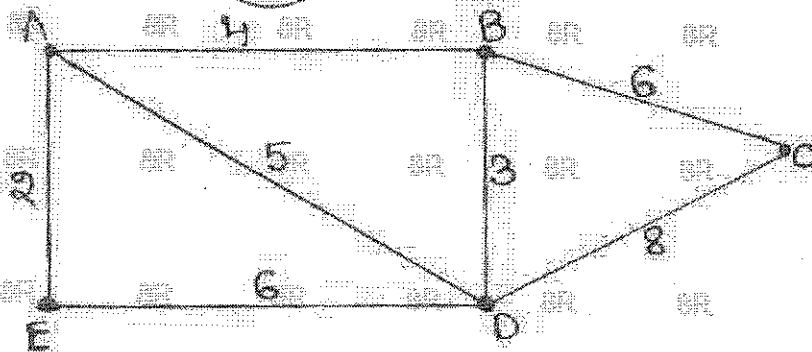
8. Solve the recurrence relation  $a_n + a_{n-1} - 8a_{n-2} - 12a_{n-3} = 0, n \geq 3$  with  $a_0 = 1, a_1 = 5, a_2 = 1$ . [10]

OR

9. Solve the following recurrence relations for a particular solution.

$$a_n - 5a_{n-1} + 8a_{n-2} - 4a_{n-3} = n2^n. \quad [10]$$

10.a) Apply Kruskal's algorithm to determine a minimal spanning tree for the weighted graph shown below:



b) Show that if a planar graph is self-dual, then  $|E| = 2|V| - 2$ . [5+5]

OR

11.a) Explain Prim's algorithm with example.

b) Use Euler's formula to show that the graph  $K_{3,3}$  is non-planar. [5+5]

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